



Analysing a two span slab using Structural Toolkit

In this tutorial:

- Slab Member Analysis using Structural Toolkit Analysis
- Slab Member Moment Capacity check using Structural Toolkit
- Slab Member Deflection check using Structural Toolkit
- Slab Member Comparison using RAPT (Reinforced And Post-Tensioned Concrete design software)

This will be a two span continuous slab (4.9m in the left span and 4.2m in the right span) with office type loading

Step 1 – Slab Member Analysis using Structural Toolkit Analysis

Using **Structural Toolkit Analysis** we will determine the positive and negative moments using pattern loads.

We will determine the maximum positive moment from the live load in the larger left span, and maximum negative moment with live loads in each adjacent span.

To start, create a new **Analysis** in **Structural Toolkit Analysis**.

Select the predefined pattern loadcase combinations.

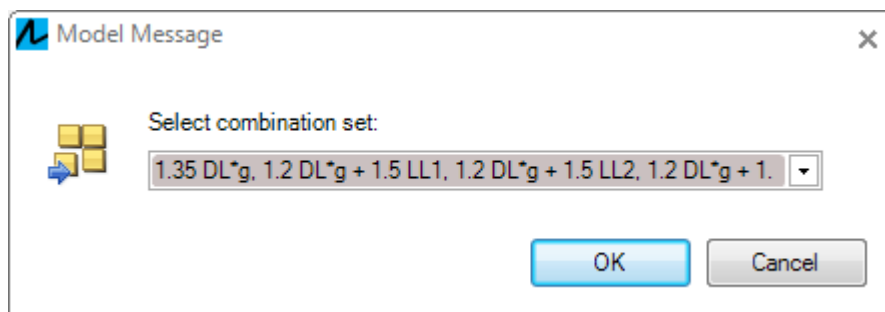


Figure 1 – Loadcase Combinations

Rename the document name to something sensible. (Remember to save the project also).

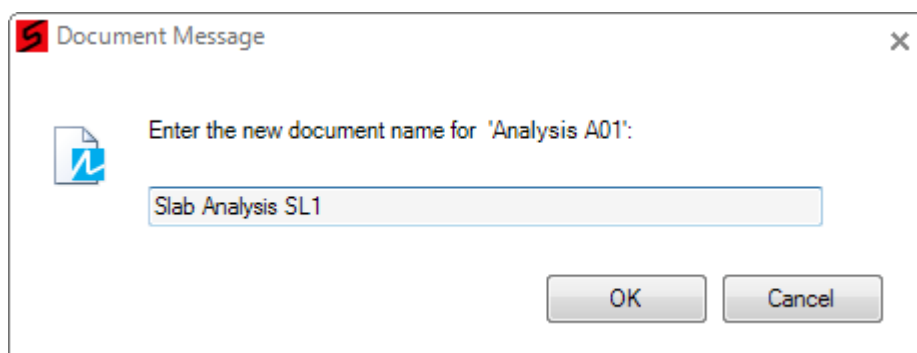


Figure 2 – Analysis Name

Enter the frame geometry

Type Ctrl-D and then hit the “0” key to bring up the input coordinate dialog.

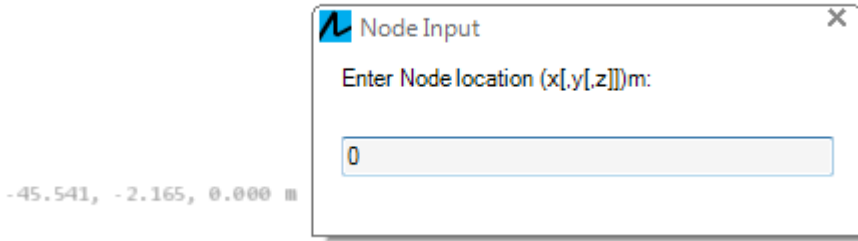


Figure 3 – Node Input Dialog

Press enter to create the node, the type “@4.9” to create the next node relative to the first node.

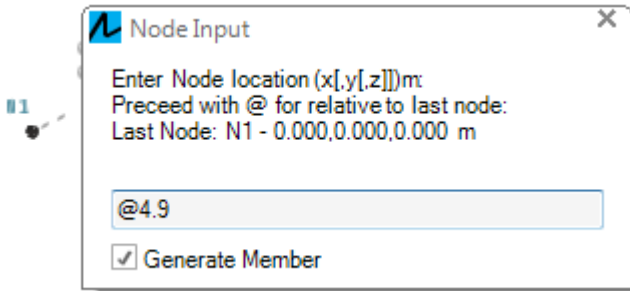


Figure 4 – Node Input Dialog (after first node)

Repeat for the next span being 4.2m.

Right click and assign a **Pinned** restraint to the left end.

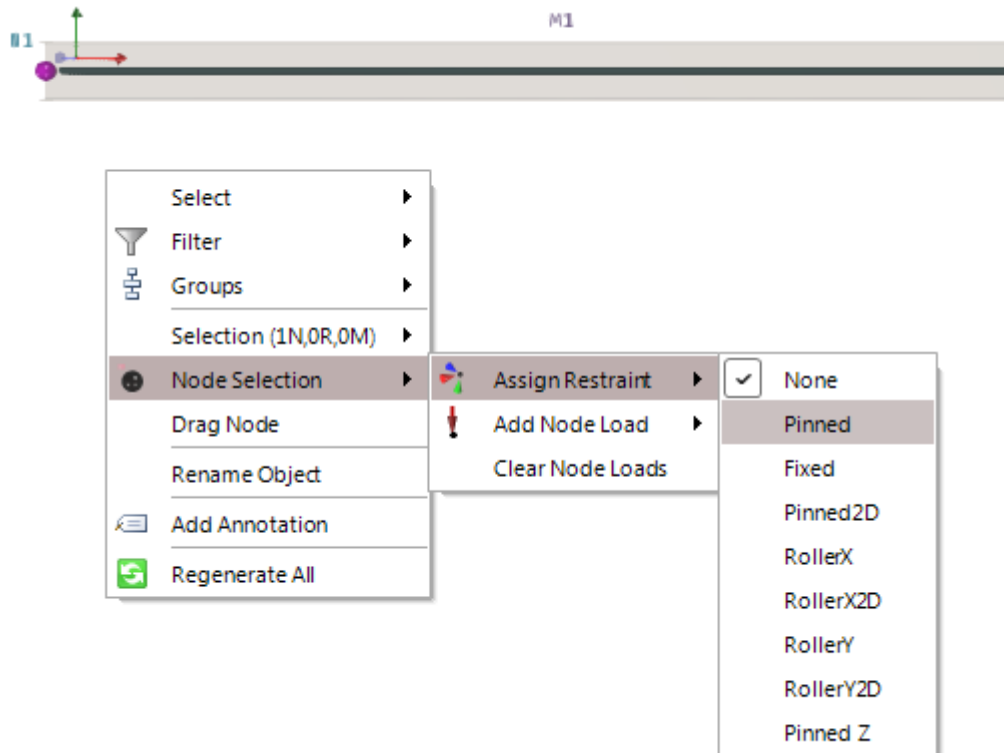


Figure 5 – Assign restraints



Assign restraints to the other two nodes using the RollerX2D. Remember to provide a pin for one support, and rollers for the others (this is not essential for a linear analysis that is horizontal, but good practise.)



Figure 6 – Beam geometry

Create the section

Enter the gross section shapes for each span. In this example we will use a 170mm thick section (x 1m strip).

First **Rename** the section for good practise.

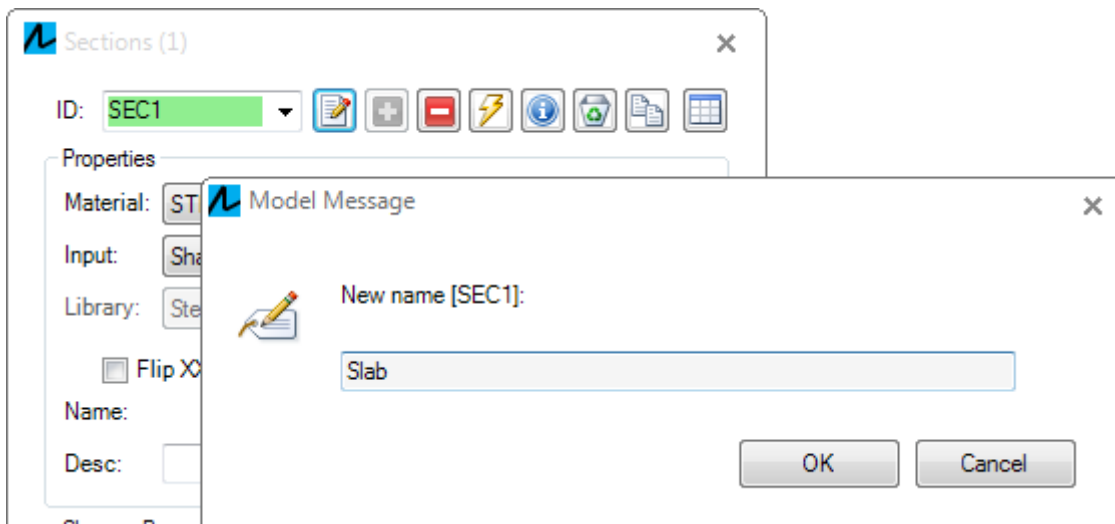


Figure 7 – Rename Section Dialog

Change the **Material** to **CONCN32** (predefined value of Concrete with 32MPa strength) and change the **Input** to **Shape**.

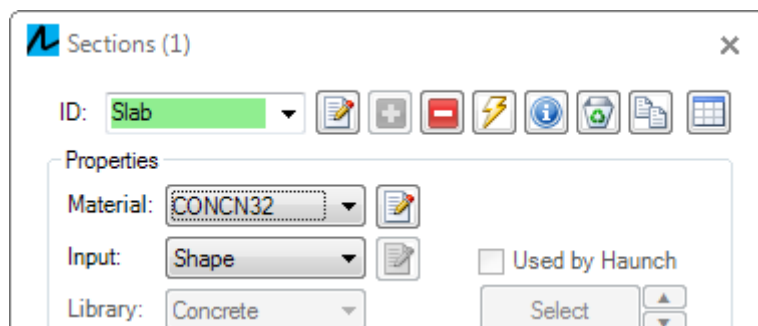


Figure 8 – Section Properties (Material)

Select the **Rect** shape for the **Profile** and assign a shape of:

D = 170mm
Bf = 1000mm

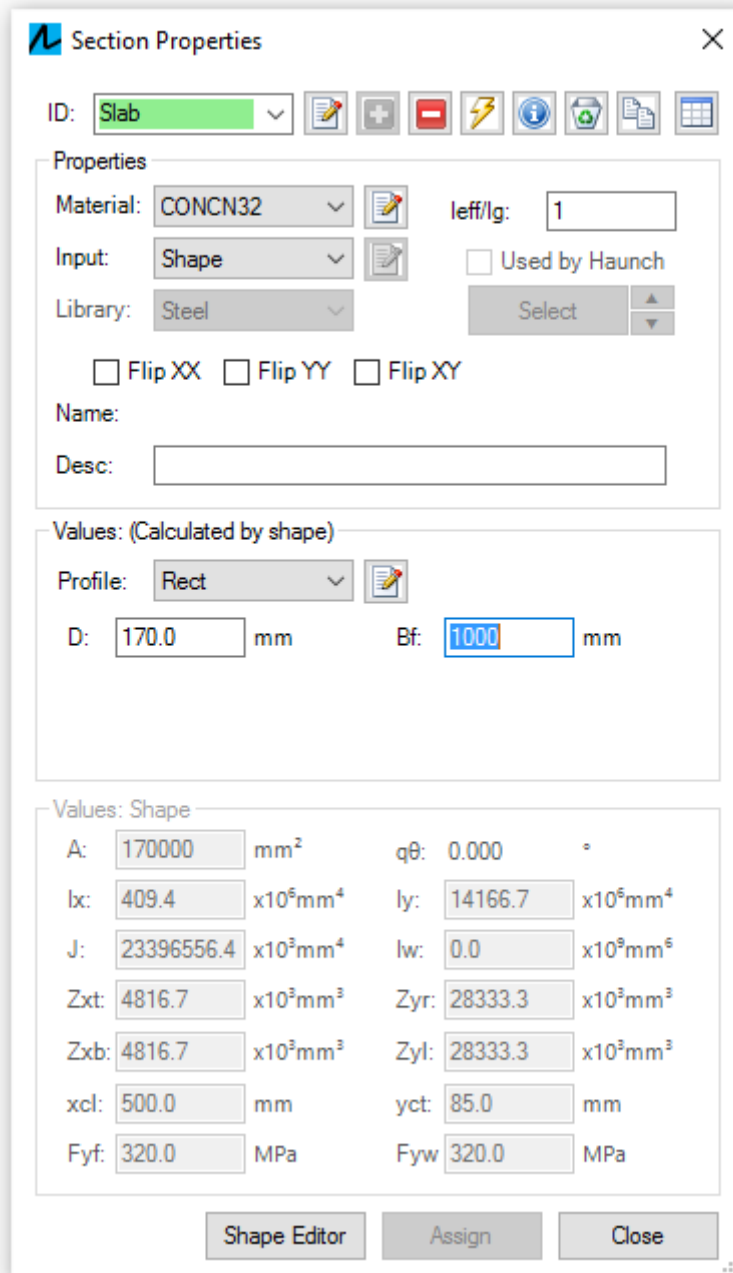


Figure 9 – Section Properties (Profile)

You may also want to open the **Material** properties and change the **Concrete Density** to 2500kg/m³ and open the **Cases** (Loadcases) and change within the **DL** case **Gravity** to -10m/s² (to have the results align with RAPT outputs for this example).

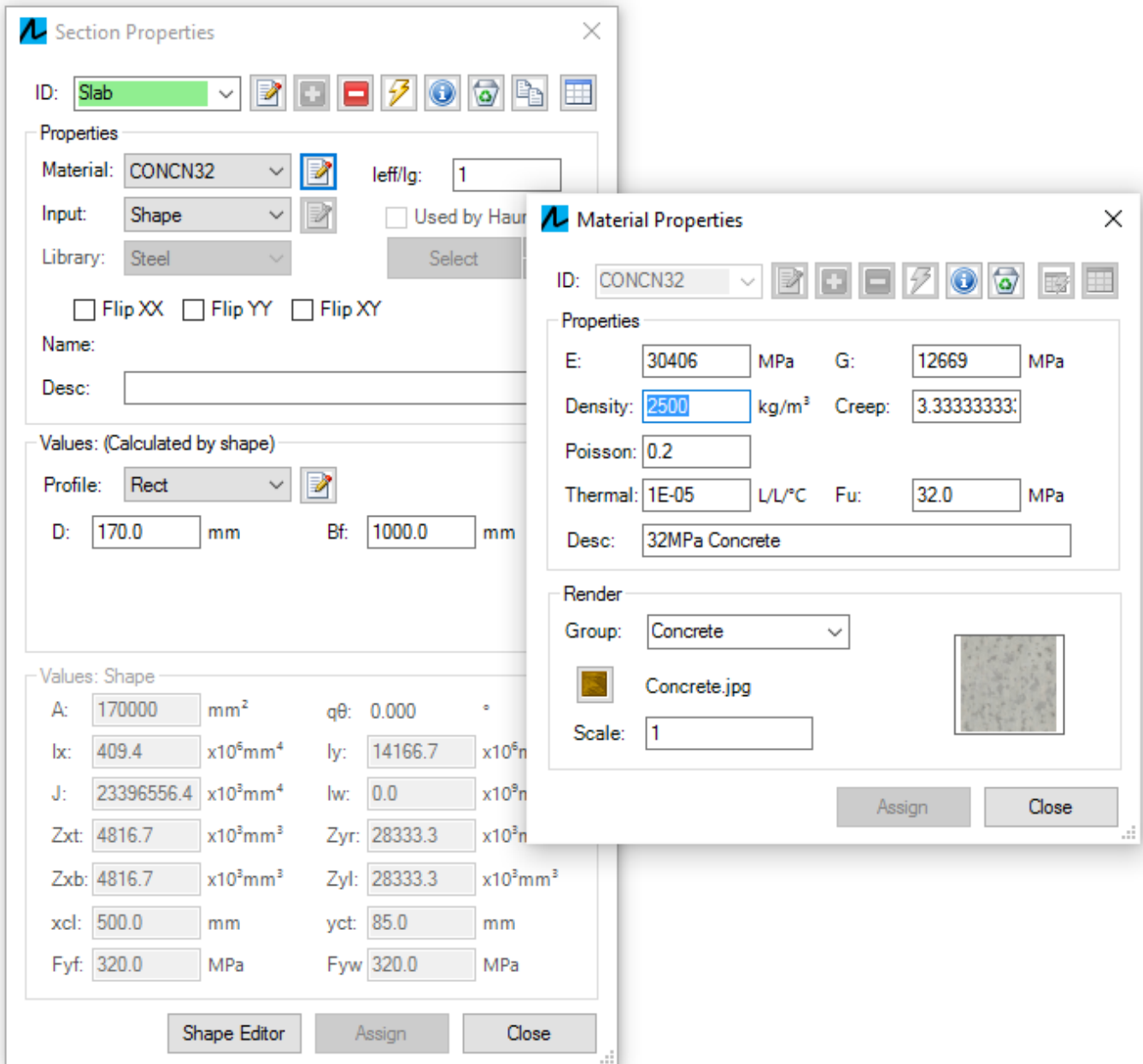


Figure 10 – Material Properties Dialog

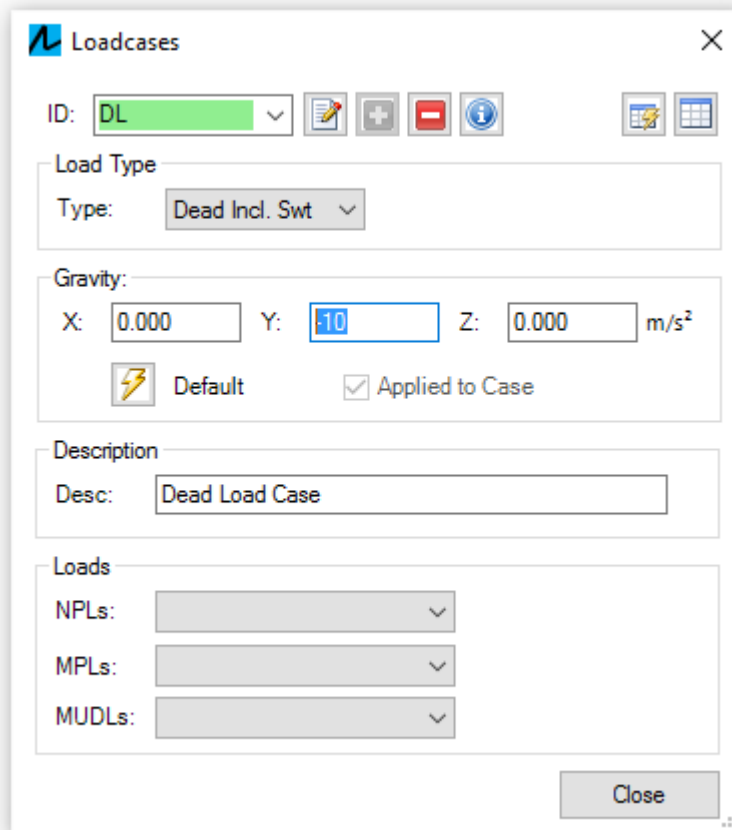


Figure 11 – Loadcases Dialog

Define the loads

Use the **Load Definitions** (below the Loads button) to define the loads.

Add a superimposed dead load of **W_{sdl} = -0.5kN**, and a live load of **W_{ll} = -(3.0 + 1.0)kN = -4.0kN**

When applying these load definitions to members, this load can be either a point loads (**kN**), or a start or end distributed load (**kN/m**).

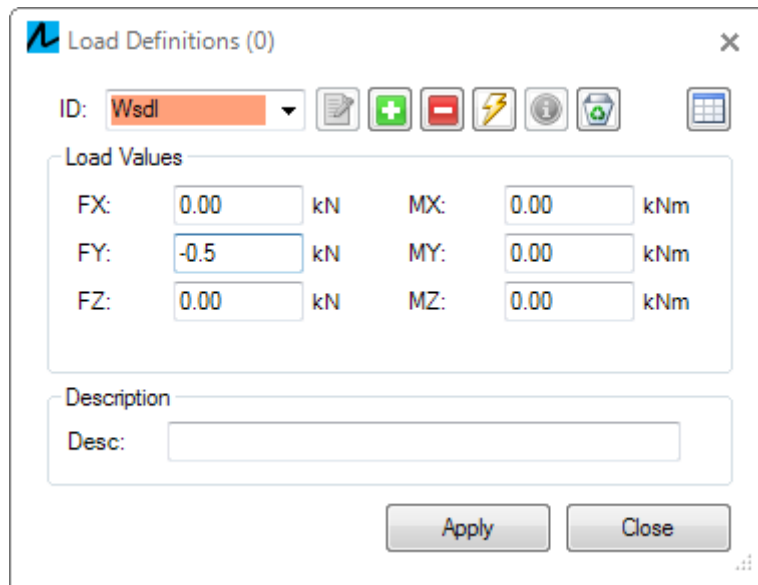


Figure 12 – Load Definitions Dialog

Change to the **DL*g** case in the Case selector in the ribbon to assign the **WsdL**.

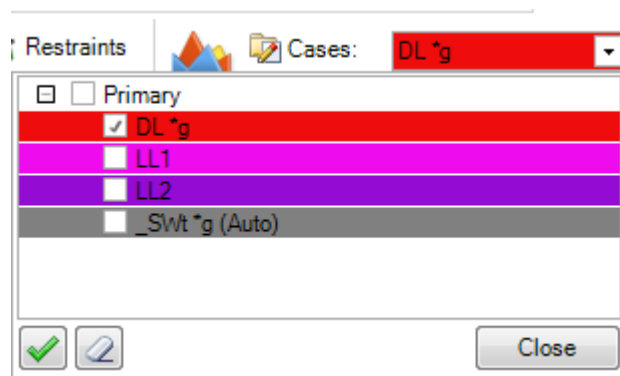


Figure 13 - Loadcases

NOTE: the **"*g"** is automatically added to cases where the gravity is applied.

Assign the load by first selecting the members, then **right click > Member Selection > Add Member UDL** and select the **WsdL** from the defined loads.

NOTE: If there are more than 10 loads defined, this right-click feature will not be available and you will need to define loads in the **Loads dialog**.

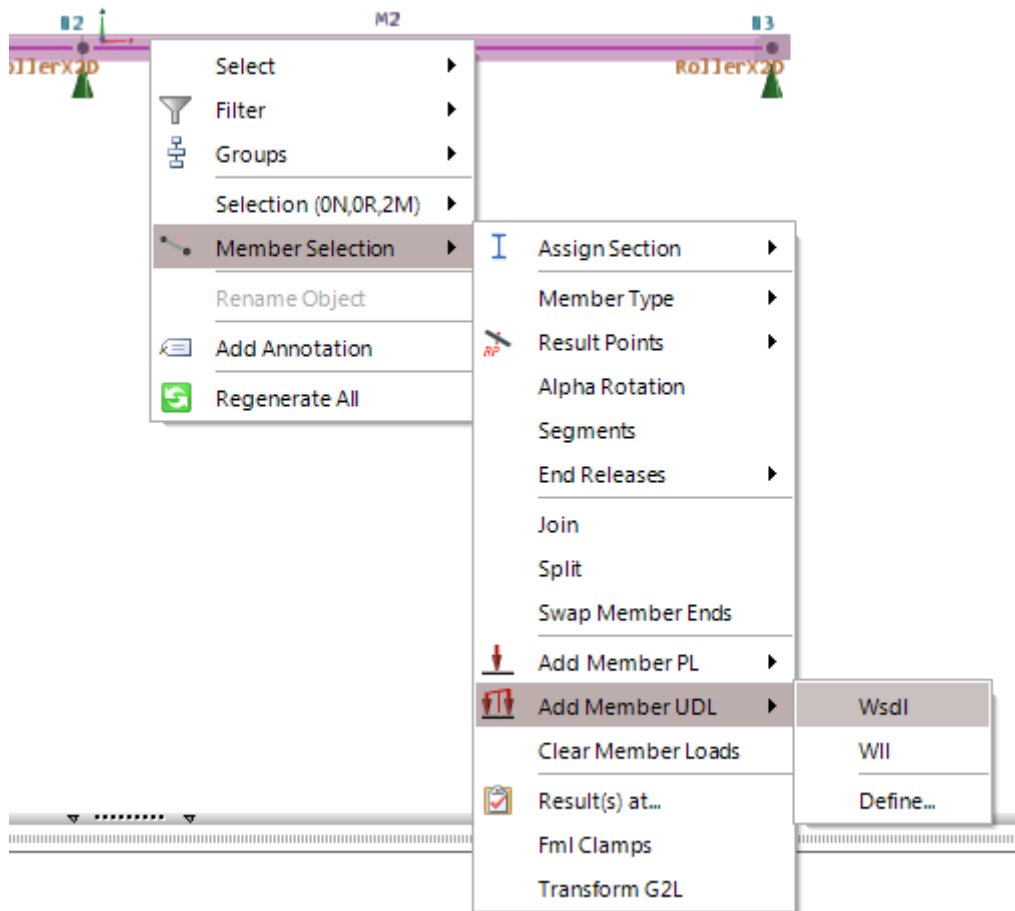


Figure 14 – Assign Member UDL

NOTE: Remember to hit the Esc key between selections to cancel the previous selection set.

Change the **Case** to **LL1** and assign the live load **WII** to the first span (**M1**).

Change the **Case** to **LL2** and assign the live load **WII** to the second span (**M2**).

Check that all loads are correctly applied by toggling through the **Cases** selector.

Analyse

Press **F5** to perform a linear analysis.

You may get a message regarding creep. This simply reminds you that the concrete long term deflections will not be calculated and the deflections are gross uncracked.

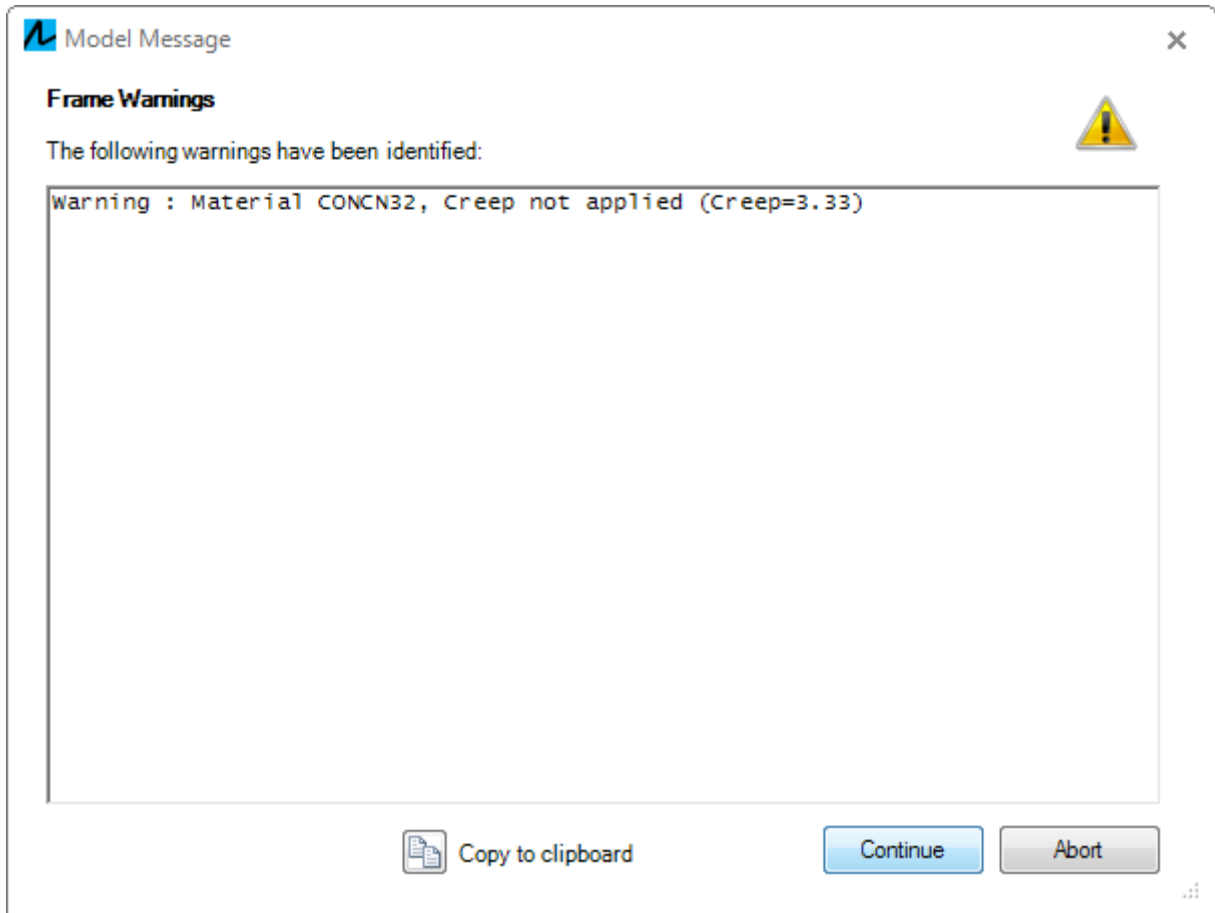


Figure 15 – Creep Warning Dialog

Press **F6** to show the Bending Moment diagram (this shows automatically on first analysis).

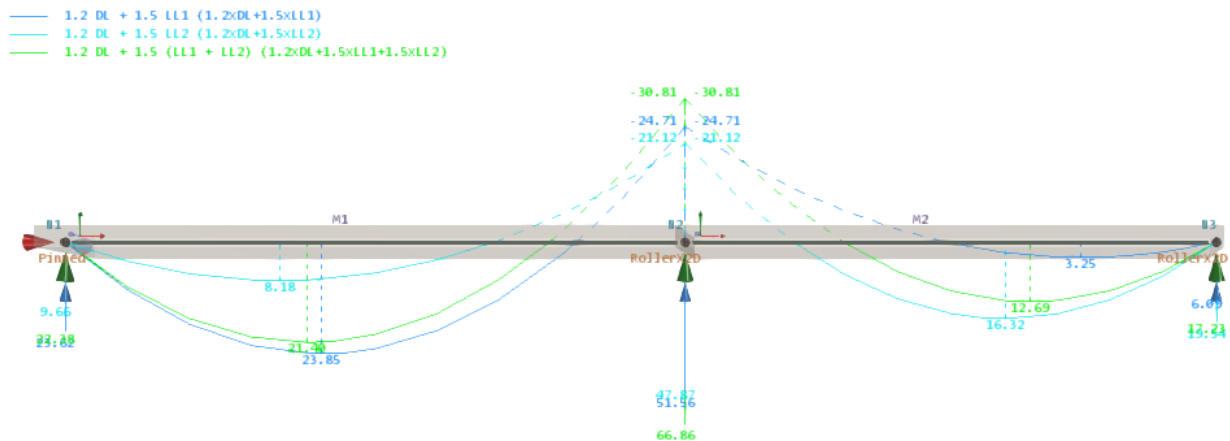


Figure 16 – Bending Moment Analysis

$M^{*+} = 30.81\text{kNm}$ (first span)
 $M^{*-} = 23.85\text{kNm}$ (at central support)



Step 2 – Slab Member Moment Capacity check using Structural Toolkit

Now we have our maximum positive and negative design moments, we can use the **Structural Toolkit Concrete Member** to check the flexural capacity.

Create a new **Concrete Member** within **Structural Toolkit** and enter the Depth (170mm), concrete strength (32MPa) and web width of “S” type representing a slab.

Geometry	S.Wt =	4.25 kN/m
Concrete strength (f _c) =		32 MPa
Span (L) =		8000 mm
Depth (D) =		170 mm
Web width (W) =		S m, (S)lab

Figure 17 – Concrete Geometry Inputs

Press the **[Analysis]** button in the side Notes section and create a linked analysis.

First, for the larger span enter a span of 4900mm, and the loads $W_{sdl} = 0.5\text{kN/m}$ and the $W_{ll} = 4.0\text{kN/m}$. Self weight is automatically calculated based on the thickness entered in the Design module.

Set the span type as “O” other to manually input the end moments and in the right side **M2***, enter the negative value at the central support. From the analysis, this is **-24.7kNm** corresponding to the greater sag case of **+23.9kNm**.



Proposed Project
Address of Project
Architect

Page:
Project No.: 15-0001
Designed: TF
Concrete Member CB01

ANALYSIS V5.00 Anthony Furr Software

Geometry for (Concrete Member CB01): beam with end moments

Description = 170mm thk slab	I _x = 409.4 x10 ⁶ mm ⁴
Span (L) = 4900 mm	A _g = 170000 mm ²
Span type = O (S)imple, (E)xterior, (I)nterior, (C)antilever, (P)ropped, (F)ixed, (O)ther	Density = 25.0 kN/m ³ (Concrete)
	E = 30024 MPa

Loading

Uniform loads	Uniform loads (kN/m)			Point loads	Point loads (kN)		
	UDL	Partial 1	Partial 2		PL 1	PL 2	PL 3
Dead load (wdl) =	0.50			Dead load (pdl) =			
Live load (wll) =	4.00			Live load (pll) =			
Start from LHS (mm) =	0			Pos. from LHS (mm) =			
End from LHS (mm) =	4900			Ultimate load (p*) =	0.00	0.00	0.00
S.Wt =	4.25	kN/m		Include S.Wt =	Y (Y)es,(N)o		
Ultimate load (w*) =	11.70	0.00	0.00	Left end (M1*) =	0.0 kNm		
Live Load type =	Floor (Concrete)			Right end (M2*) =	-24.7 kNm		
Short term LL (Ψ _{su}) =	0.70	(Ψ _{sp}) =	1.00	Position of result (x) =	2450 mm		
Long term LL (Ψ _{lu}) =	0.40	(Ψ _{lp}) =	0.40				
Actual LL (Ψ _{sa}) =	0.70	(Ψ _{la}) =	0.40				

Results at midspan

1.20*G+1.50*Q analysed - 1.35*G case to be checked

	Left	At x	Right	Max	At	Min	At	Units
R _{dI}	9.59		13.68					kN
R _{lI}	8.08		11.52					kN
R*	23.62		33.71					kN
M*	0.00	22.76	-24.70	23.85	2015	-24.70	4900	kNm
V*	23.62	-5.04	-33.71	33.71	4900			kN
δ _{dI}	0.00	1.68	0.00	1.68	2450	0.00	0	mm
δ _{lI}	0.00	1.41	0.00	1.41	2450	0.00	0	mm
δ _{dI} +Ψ _s *δ _{lI}	0.00	2.66	0.00	2.66	2450	0.00	0	mm

δP_{II}/δTot.II = 0.00

Graphs * Deflections are Gross I_g immediate - assessment of long term effects to be considered

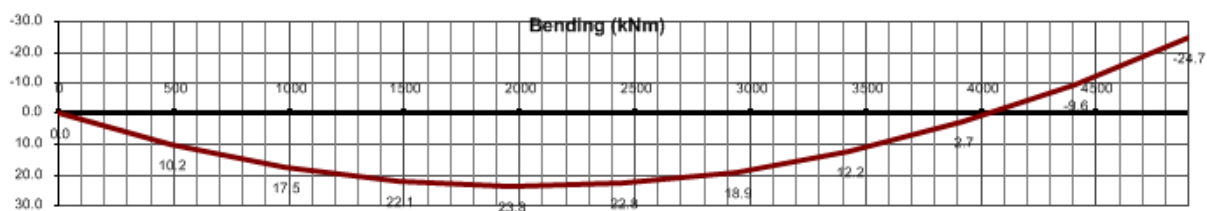



Figure 18 – Analysis Module

Press the **[Switch to Design...]** button in the side Notes area to return to the **Concrete Member** design module.

Press the **[Max M+*]** to begin designing the section for the positive moment and enter bar sizes of 12mm and at centres of 250mm (**N12-250**) as the bottom reinforcement with 20mm bottom cover, and bar sizes of 12mm at centres of 300mm (**N12-300**) as the top steel, again with 20mm cover.







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Proposed Project
Address of Project
Architect

Page:
Project No.: 15-0001
Designed: TF

Concrete Member CB01

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Section: (Concrete Member CB01) 170mm thk slab, f'c=32MPa

Reinf't: N12-300 cts top, N12-250 cts bottom, ku = 0.07

Strength: (+ve M) M* = 23.9kNm < φMuo = 24.8kNm (φMuo.min = 16.3kNm) OK (0.96)
Ast.req'd = 426mm² (N12-260)

Cracking: fscr = 252MPa < Fscr = 297MPa & fscr1 = 292MPa < Fscr1 = 400MPa OK (0.73,0.85)

Ast.min: Ast.min = 272mm² < Ast = 452mm² (Minimum of Deemed and actual) OK (0.60)

Geometry S.Wt = 4.25 kN/m L/D ratio = 28.8

Concrete strength (f'c) = 32 MPa

Depth (D) = 170 mm

Web width (W) = 5 mm, (S)lab

Comp.
 Tension

Slab type = 0 (O)ne way, Two way & (C)ols, (T)wo way & walls, (F)ooting

Formwork = S (S)tandard, (R)igid

Concrete weight = 25.0 kN/m³ Exposure Top = A1 Tab 4.10.3.2

Fully enclosed = N (Y)es, (N)o Bottom = A1 Tab 4.10.3.2

Gross area (Ag) = 170000 mm²

Analysis: beam with end moments at 2015mm from LHS (Max +ve M)

Analysis values = X (M)anual, (L)eft, Position (X) from analysis, (R)ight

Refer to the analysis output

	Left	Max+	Right	Units
M*	0.0	23.9	-24.7	kNm
Ms1*	0.0	17.8	-18.5	kNm
Ms*	0.0	15.4	-15.9	kNm
Ast req'd	0	426	442	mm ² /m
Ast	452	452	377	mm ² /m
Reinf't req'd	-	N12-260	N12-250	

Reinforcement

Bottom steel = N12-250 cts

Bar size = 12 mm

Bar cts/No/mm² = 250

Yield strength (fsy) = 500 MPa

Bottom cover to steel = 20 mm

Steel area (Ast) = 452 mm²/m

Ductility class = A (N)ormal, (L)ow, (A)uto

Reinf't ductility class = N (N)ormal, (L)ow

Depth to bottom steel layer (ds.max) = 144 mm

Top steel = N12-300 cts

Bar size = 12 mm

Bar cts/No/mm² = 300

Yield strength (fsyc) = 500 MPa

Top cover to steel = 20 mm

Steel area (Asc) = 377 mm²/m

Ductility class = A (N)ormal, (L)ow, (A)uto

Reinf't ductility class = N (N)ormal, (L)ow

Depth to top steel layer = 26 mm

Figure 19 – Concrete Module (Positive Moment Check)

The summary at the top indicates that the section capacity is **OK** for the positive moment case.

For the negative bending, we can not simply transfer the moment, because the pattern load we have input into the Analysis module was for the maximum deflection and sage case. So we need change the **Analysis values** to “M” manual method and enter the –ve moment of M* = -30.8kNm.





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Section: (Concrete Member CB01) 170mm thk slab, $f'_c=32\text{MPa}$
 Reinf't: N12-200 cts top, N12-400 cts bottom, $k_u = 0.09$
 Strength: (-ve M) $M^* = 30.8\text{kNm} < \phi M_{uo} = 31.0\text{kNm}$ ($\phi M_{uo, \text{min}} = 16.4\text{kNm}$) OK (0.99)
 Ast.req'd = 556mm^2 (N12-200)
 Cracking: $f_{scr} = 264\text{MPa} < F_{scr} = 297\text{MPa}$ & $f_{scr1} = 304\text{MPa} < F_{scr1} = 400\text{MPa}$ OK (0.76,0.89)
 Ast.min: Ast.min = $272\text{mm}^2 < A_{st} = 565\text{mm}^2$ (Minimum of Deemed and actual) OK (0.48)

Geometry S.Wt = 4.25 kN/m L/D ratio = 47.1

Concrete strength (f'_c) = 32 MPa
 Span (L) = 8000 mm
 Depth (D) = 170 mm
 Web width (W) = S mm, (S)lab



Comp.
 Tension

Slab type = O (O)ne way, Two way & (C)ols, (T)wo way & walls, (F)ooting
 Formwork = S (S)tandard, (R)igid
 Concrete weight = 25.0 kN/m³ Exposure Top = A1 Tab 4.10.3.2
 Fully enclosed = N (Y)es, (N)o Bottom = A1 Tab 4.10.3.2
 Gross area (A_g) = 170000 mm²

Design actions

Analysis values = M (M)anual, (L)eft, Position (X) from analysis, (R)ight

Manual values	Manual	Units
Design (M^*) = -30.8 kNm/m	M^* -30.8	kNm
Design (M_{s1}^*) = d kNm/m	M_{s1}^* -23.1	kNm
Design (M_{s^*}) = d kNm/m	M_{s^*} -20.0	kNm
	Ast req'd	556 mm ²
	Ast	565 mm ²
	Reinf't req'd	N12-200

Estimates for M_{s1}^* and M_{s^*} used - To be verified

Reinforcement

Bottom steel = N12-400 cts		Top steel = N12-200 cts	
Bar size = 12 mm	<input type="text" value="12"/> Mesh...	Bar size = 12 mm	<input type="text" value="12"/> Mesh...
Bar cts/No/mm ² = 400 mm	<input type="text" value="400"/>	Bar cts/No/mm ² = 200 mm	<input type="text" value="200"/>
Yield strength (f_{sy}) = 500 MPa	<input type="text" value="500"/>	Yield strength (f_{syc}) = 500 MPa	<input type="text" value="500"/>
Bottom cover to steel = 20 mm	<input type="text" value="20"/>	Top cover to steel = 20 mm	<input type="text" value="20"/>
Steel area (A_{sc}) = 283 mm ² /m	<input type="text" value="283"/>	Steel area (A_{st}) = 565 mm ² /m	<input type="text" value="565"/>
Ductility class = A (N)ormal, (L)ow, (A)uto	<input type="text" value="A"/>	Ductility class = A (N)ormal, (L)ow, (A)uto	<input type="text" value="A"/>
Reinf't ductility class = N (N)ormal, (L)ow	<input type="text" value="N"/>	Reinf't ductility class = N (N)ormal, (L)ow	<input type="text" value="N"/>
Depth to bottom steel layer ($d_{s, \text{max}}$) = 144 mm	<input type="text" value="144"/>	Depth to top steel layer = 26 mm	<input type="text" value="26"/>
Depth to bottom steel (d_s) = 144 mm	<input type="text" value="144"/>	Depth to top steel = 26 mm	<input type="text" value="26"/>
D-ds = 26 mm	<input type="text" value="26"/>	D-ds = 144 mm	<input type="text" value="144"/>
No. bars = 2.5 No.	<input type="text" value="2.5"/>	No. bars = 5.0 No.	<input type="text" value="5.0"/>

Figure 20 – Concrete Module (Negative Moment Check)

Enter the top reinforcement of 12mm bars at 200mm centres (N12-200), and the bottom reinforcement of 12mm bars at 400mm centres (N12-400) (cover as previous).

The summary at the top indicates that the section capacity is **OK** for the negative moment case.





Step 3 – Slab Member Deflection check using Structural Toolkit

To check the deflections, we first we need to set up the reinforcement again for this span.

Enter the **N12-250 bars** in the bottom and **N12-200 bars** in the top on the **[Design]** sheet.


Go to the **[Defl]** tab and press the **[Max. Deflection]** button in the Notes.

Press the **[Transfer Reinf't]** to transfer the reinforcement to the Defl tab. Note that some of the reinforcement areas do not transfer as the steel is in a compression zone which is in tension.

NOTE: If you enter the value manually in the middle span top reinforcement you will notice an error message further down advising that the top compression reinforcement is actually in tension and should be ignored.

NOTE: Ensure you go to the **[Shrink & Creep]** tab to set the exposure and location of the slab (ie. Environment and City) which will affect the σ_{cs} which in turn affects M_{cr} which then alters the deflections.





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Proposed Project
Address of Project
Architect

Page:
Project No.: 15-0001
Designed: TF

Concrete Member CB01

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Section: (Concrete Member CB01) 170mm thk slab, f'c=32MPa
Reinf't: N12-200 cts top, N12-250 cts bottom (Additional reo specified)
Def'n: δ.di = 6.4mm, δ.ll = 1.9mm, δ.inc = 10.4mm, δtotal = 13.6mm (span / 359) OK
 ocs for Interior environment with εcsd.b*=1000x10⁻⁶ ±30%, εcs*=672x10⁻⁶

Deflections - Cl 8.5.3 beam with end moments at midspan (Max +ve Def)

Concrete density (ρ) =	2400 kg/m ³ Cl 3.1.3	Gross area (Ag) =	170000 mm ²
Use fcmi? =	Y (Y)es,(N)o	Uncr.g. neutral axis (NA) =	85 mm from top
fcmi =	35.3 MPa	Gross Stiffness (I _g) =	409 x10 ⁶ mm ⁴ (w/o reinf't)
Deflection at =	X (M)anual, (C)ritical, (L)eft, Position (X) from analysis, (R)ight	Steel Modulus (Es) =	200000 MPa Cl 3.2.2
Position (x) =	2450 mm	Mod. of elast. (Ec = ρ ^{1.5} *0.043*√fcmi) =	30024 MPa ± 20% Cl 3.1.2
Span type =	O	Modular ratio (n = Es/Ec) =	6.661

Deflection calculation

	Left	At x	Right	Units
Manual (M*) =				kNm
Manual (Ms*) =				kNm
Analysis (M*) =	0.0	22.8	-24.7	kNm
Analysis (Ms*) =	0.0	14.7	-15.9	kNm
Top Steel:				
Ast req'd =	0	0	442	mm ² /m
Design Ast =	565		565	mm ² /m
Ast =	0	0	565	mm ² /m
			N12-200	
Bottom steel:				
Ast req'd =	0	406	0	mm ² /m
Design Ast =	452	452		mm ² /m
Ast =	0	452	0	mm ² /m
			N12-250	
Uncracked NA =	85	86	84	mm
Uncracked uk =	1.000	1.021	1.027	x10 ⁶ mm ⁴
I _{uncr} = uk*W*D ³ /12 =	409	418	420	x10 ⁶ mm ⁴
Tensile steel (Ast) =	0	452	565	mm ² /m
Depth to ds =	144	144	144	mm (From comp. face)
Comp. steel (Asc) =	0	0	0	mm ² /m
dc =	26	26	26	mm (From comp. face)
Cracked κ =	0.000	0.185	0.204	mm
Depth to cracked NA = κ*ds =	0.0	26.6	29.4	mm (From top)
Use Comp. steel =	-	-	-	
yt =	85	84	84	mm (From tensile fibre)
Design shrinkage εcs* =	672	672	672	x10 ⁻⁶ ±30% Interior env. refer Shrinkage tab
W (slab) =	1000	1000	1000	mm
Tension steel ratio (pw=Ast/(ds*W)) =	0.0000	0.0031	0.0039	
Comp. steel ratio (pcw=Asc/((D-dc)*W)) =	0.0000	0.0000	0.0000	
σcs =	0.00	0.91	1.10	MPa
Mcr = (f'ct.f-σcs)*I _g /yt =	16.3	12.3	11.5	kNm
Cracked κc =	0.000	0.192	0.233	
I _{cr} = κc*W*ds ³ /12 =	0	48	58	x10 ⁶ mm ⁴
I _{ef,max} =	246	246	246	x10 ⁶ mm ⁴
I _{ef} =	0	246	193	x10 ⁶ mm ⁴
I _{av} = (M + R) / 2 value =	220x10 ⁶ mm ⁴			
Ratio I _{uncr} /I _{av} =	1.90 I _{uncr} at position x			
kcs = [2-1.2*(Asc/Ast)] ≥ 0.8 =	2.000 kcs at position x			

Deflection summary - Located at midspan (Max +ve Def)

		Manual Values:
Gross δdl.g.imm =	1.7 mm	Gross δdl.g.imm = 1.26 mm
Gross δll.g.imm =	1.4 mm	Gross δll.g.imm = 1.47 mm
Short term δ.short = [δdl.g+ψs*δll.g]*I _{uncr} /I _{ef} =	5.1 mm	Short term δdl.short = 3.2 mm
Sustained δ.sus = [δdl.g+ψl*δll.g]*I _{uncr} /I _{ef} =	4.3 mm	Short term δll.short = 1.9 mm
Long term δ.long = kcs*δ.sus =	8.5 mm	Long term δdl.long = 6.4 mm
Incremental δ.inc = δ.long + δll.short =	10.4 mm	Long term δll.long = 2.2 mm
		Total δdl.total = 11.7 mm
Total δ.total = δ.short + δ.long =	13.6 mm	Span / 359

Deflection limits

δDL lim. = Span/	250 = 20mm or	mm	δDL lim. =	20 mm
δLL lim. = Span/	300 = 16mm or	mm	δLL lim. =	16 mm
δinc lim. = Span/	250 = 20mm or	mm	δLL inc. =	20 mm
δTot. lim. = Span/	250 = 20mm or	mm	δTot. lim. =	20 mm

Figure 21 – Concrete Module, Deflections





The Concrete Member module calculates a total deflection of 13.6mm. This compares to the RAPT output of 14mm total deflection (see Appendix A).

END OF TUTORIAL

V5.0.1.2



Appendix A - RAPT Comparison

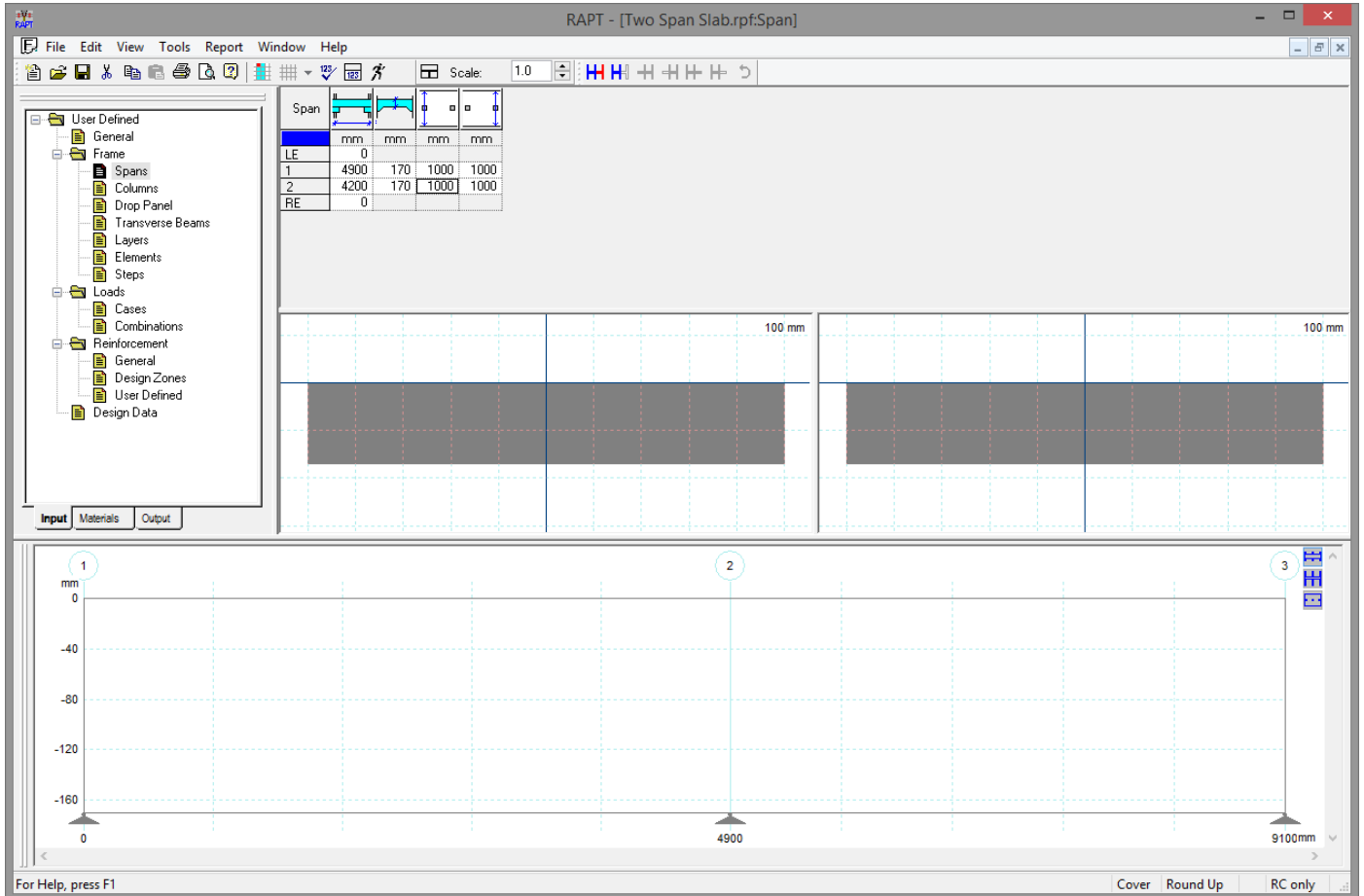


Figure A1 – Rapt Frame Geometry

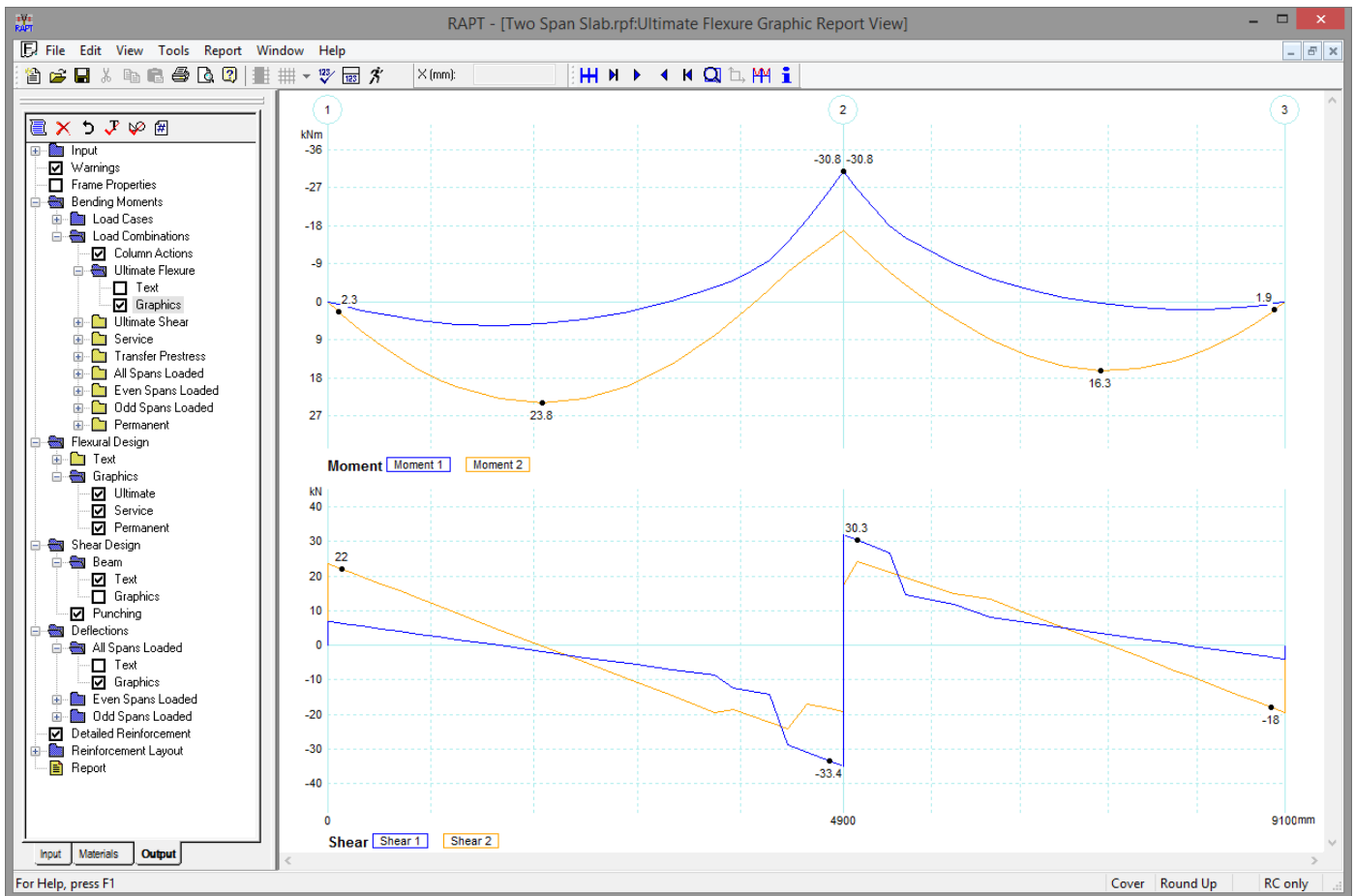


Figure A2 – Shear Force Diagram

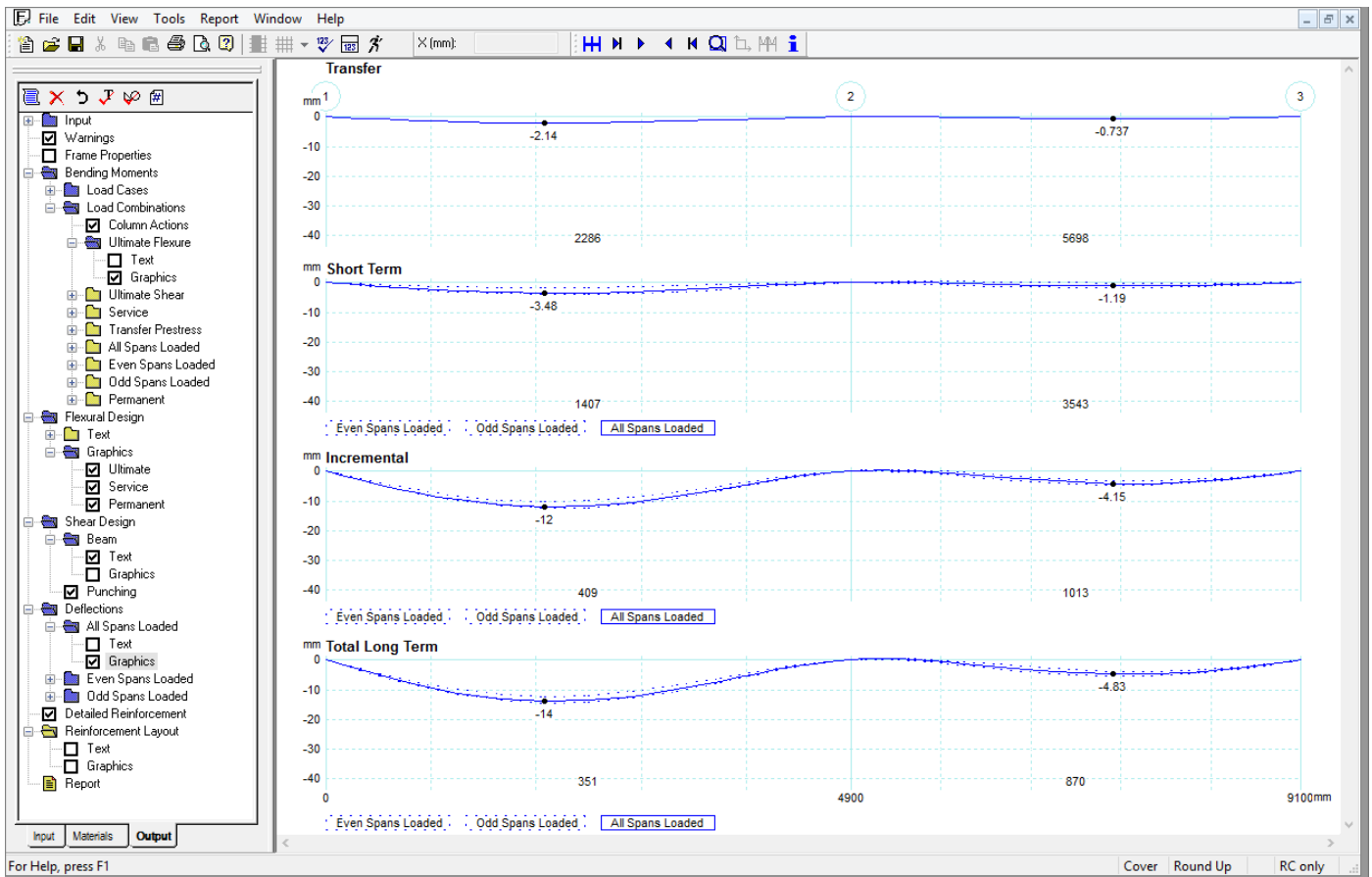


Figure A3 - Deflections

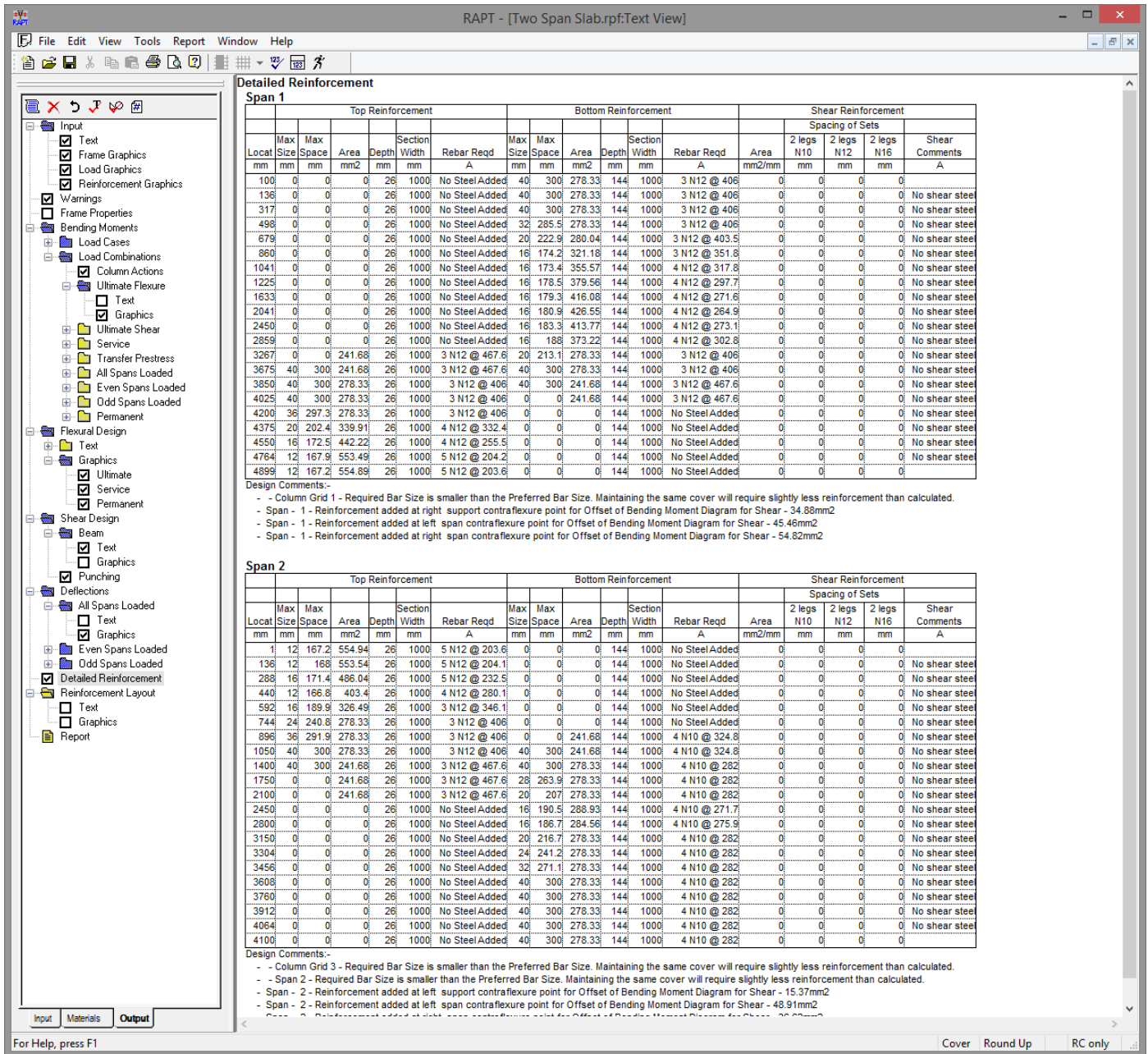


Figure A4 – Reinforcement Output

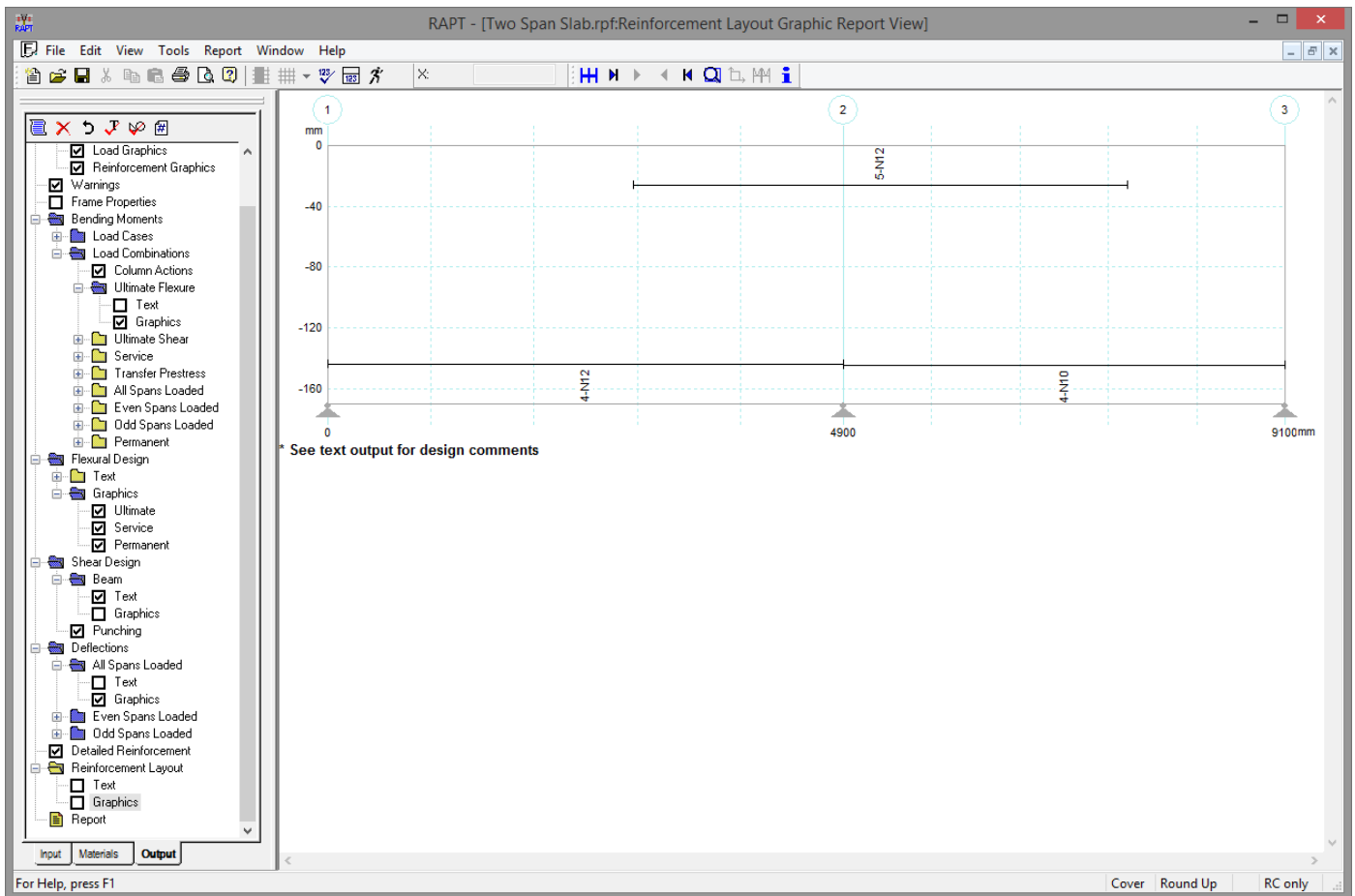


Figure A5 – Reinforcement Diagram